

CONCEPT: PROTEIN-LIGAND FRACTIONAL SATURATION

Fraction of Ligand-Binding-Sites Occupied by Ligand (θ)

- Fractional saturation (θ or Y): fraction of _____ (or *saturated*) ligand-binding-sites in a protein sample.
- θ : ratio of *occupied proteins* to *total protein*; reveals _____ (%) of *occupied* ligand-binding-sites on a protein.
 - Values of θ range from _____ (when *no L* is bound) to _____ (when *all* binding sites are bound by *L*).
 - Recall: $K_d = [L]$ when $\theta =$ _____, or _____% of all the available ligand-binding-sites are *occupied* by ligand.
 - Saturation curves or *Protein-ligand-binding graphs* plot _____ on the y-axis and $[L]$ on the x-axis.

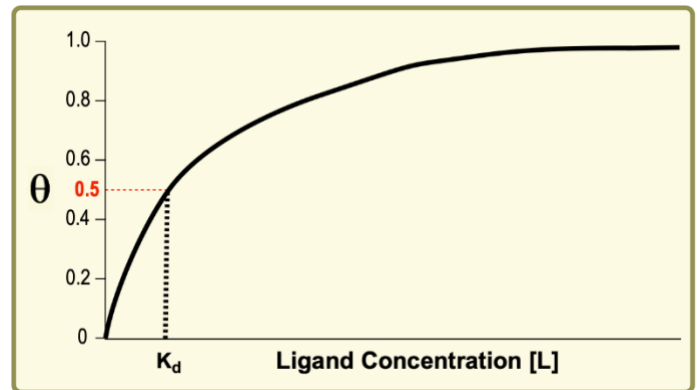
EXAMPLE: Protein-Ligand-Binding Plot.

$$\theta = Y = \frac{\text{Protein Binding Sites bound by Ligand}}{\text{Total Protein Binding Sites}} = \frac{[PL]}{[PL] + [P]}$$

Recall:

Rectangular Hyperbola Equation:

$$y = \frac{aX}{X + b}$$

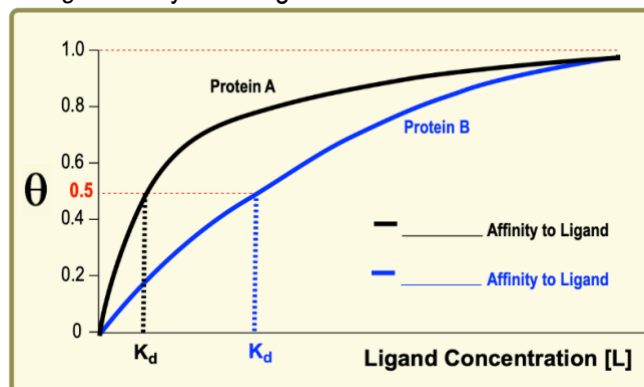


Max θ

- For *ALL* protein-ligand interactions, the equivalent of the " V_{\max} " is 100% *L*-binding (max $\theta =$ _____).
- Recall: V_{\max} is subject to change with different enzymes; HOWEVER, max θ is *always* _____.
- Recall: K_m is similar to K_d , so the _____ the K_d value, the *stronger* the protein's affinity for that ligand.

EXAMPLE: Which protein has a *stronger* affinity to the ligand?

- Protein A.
- Protein B.



- Through *algebraic rearrangements & substitutions* of previous equations, θ can also be defined in another way:
 - This mathematically relates θ to _____ AND it *resembles* the Michaelis-Menten Equation.

$$\theta = Y = \frac{[PL]}{[PL] + [P]} = \frac{() [L]}{[L] + K_d}$$

$$"V_{\max}" = \text{Max } \theta = 1$$

Michaelis-Menten Equation:

$$V_0 = \frac{V_{\max} [S]}{[S] + K_m}$$

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EXAMPLE: If an antibody binds to an antigen (ligand) with a K_d of 5×10^{-8} M, what concentration of antigen will $\theta = 0.2$?

- a) 1.25×10^{-8} M. c) 3.8×10^{-4} M.
- b) 1.25×10^{-6} M. d) 2.1×10^{-2} M.

PRACTICE: Which of the following statements about protein-ligand binding is correct?

- a) The K_a is equal to the concentration of ligand when all the binding sites are occupied.
- b) The larger the K_a , the stronger the affinity a protein has for its ligand.
- c) The larger the K_a , the faster the binding.
- d) The K_a is independent of conditions including salt concentrations and pH.

PRACTICE: Consider the following graph for parts A-C.

A) What is the protein-ligand dissociation constant (K_d) for protein X?

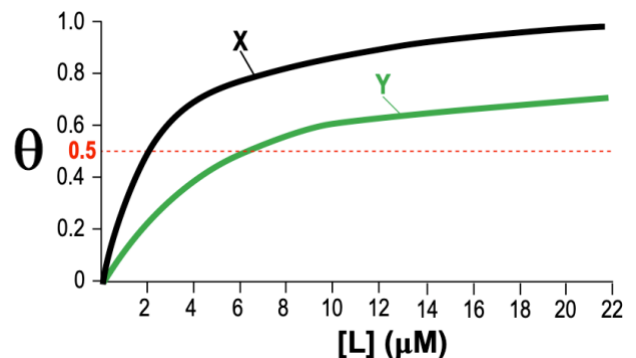
- a) 2 μ M. b) 4 μ M. c) 6 μ M. d) 8 μ M.

B) What is the protein-ligand dissociation constant (K_d) for protein Y?

- a) 2 μ M. b) 4 μ M. c) 6 μ M. d) 8 μ M.

C) Which protein has a greater affinity for ligand A?

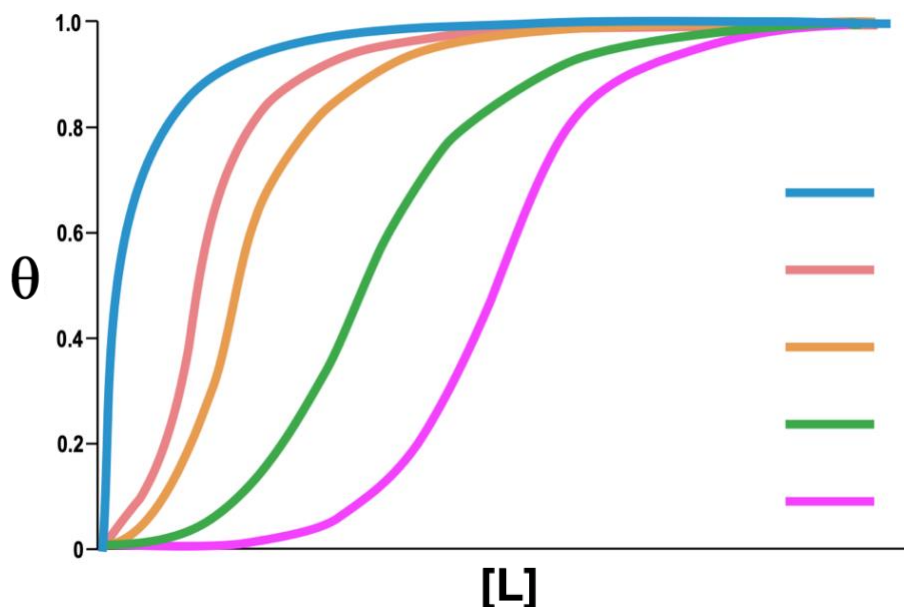
- a) Protein X. b) Protein Y.



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PRACTICE: Match the dissociation constants in the table below to the appropriate curves on the graph.

Protein Name	K_d (M)
A	2×10^{-6}
B	1×10^{-7}
C	1×10^{-6}
D	4×10^{-8}
E	9×10^{-7}



PRACTICE: Use the table below to answer questions A, B & C below.

A) Which protein has a greater affinity for their ligand?

- a) Protein 1.
- b) Protein 2.

[Ligand] (nM)	q of Protein 1	q of Protein 2
0.5	0.2	0.05
1	0.5	0.2
2	0.8	0.5
3	0.9	0.8

B) According to the data in the table, what is the dissociation constant (K_d) for Protein 1?

Protein 1 K_d = _____

C) According to the data in the table, what is the association constant (K_a) for Protein 2?

Protein 2 K_a = _____

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PRACTICE: A sample of cells has a total protein-receptor concentration of 10 mM. 25% of the protein-receptors are occupied with ligand when the concentration of free ligand is 15 mM. Calculate the K_d for the receptor-ligand interaction.

- a) 5 mM.
- b) 67 mM.
- c) 45 mM.
- d) 7.5 mM.
- e) 2.5 mM.