

## TOPIC: POWERS OF $i$

- Recall:  $i = \sqrt{-1}$ . Many problems will have  $i$  raised to the 2<sup>nd</sup>, 3<sup>rd</sup>, or even much higher powers!
  - All properties of exponents can be applied to powers of  $i$

POWERS OF $i$	
$i^1 = \longrightarrow \rightarrow$ _____	$i^5 = \_\_\_\_\_ = \_\_\_\_\_ = \_\_\_\_\_$
$i^2 = \longrightarrow \rightarrow$ _____ = _____	$i^6 = \_\_\_\_\_ = \_\_\_\_\_ = \_\_\_\_\_$
$i^3 = \_\_\_\_\_ = \_\_\_\_\_ = \_\_\_\_\_$	$i^7 = \longrightarrow \rightarrow$ _____
$i^4 = \_\_\_\_\_ = \_\_\_\_\_ = \_\_\_\_\_$	$i^8 = \longrightarrow \rightarrow$ _____

- Any power of  $i$  can **ALWAYS** be simplified to \_\_\_\_, \_\_\_\_, \_\_\_\_, or \_\_\_\_

### How To Evaluate Higher Powers of $i$

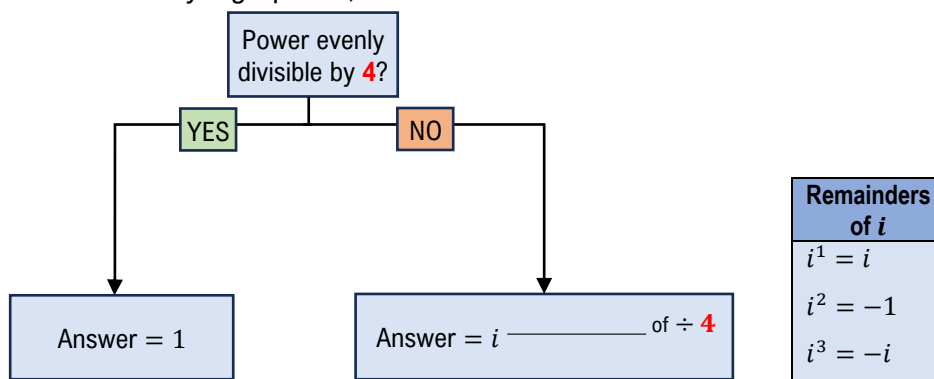
- We can express powers of  $i$  in terms of \_\_\_\_.

EXAMPLE: Simplify the power of  $i$ .

$$\begin{aligned}
 (A) \quad i^{20} &= i^4 \cdot i^4 \cdot i^4 \cdot i^4 \cdot i^4 \\
 &= 1 \cdot 1 \cdot 1 \cdot 1 \cdot 1 \\
 &=
 \end{aligned}$$

$$\begin{aligned}
 (B) \quad i^{22} &= \underbrace{i^4 \cdot i^4 \cdot i^4 \cdot i^4 \cdot i^4}_{\text{}} \cdot i^2 \\
 &= \\
 &=
 \end{aligned}$$

- To evaluate  $i$  raised to a *very high* power, here's a shortcut:



EXAMPLE: Simplify the power of  $i$ .

$$(A) \quad i^{100}$$

$$(B) \quad i^{22}$$

$$(C) \quad i^{67}$$

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PRACTICE: Simplify the power of  $i$ .

$$i^{1003}$$

Remainders of $i$
$i^1 = i$
$i^2 = -1$
$i^3 = -i$

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PRACTICE: Simplify the power of  $i$ .

$$i^{85}$$