

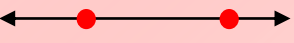


TOPIC: LINEAR INEQUALITIES

Interval Notation

- Instead of set notation, a more compact way to express solution sets is in **interval notation**.

$$\{x \mid -13 < x \leq 9\}$$

$$(-13, 9]$$

	CLOSED INTERVAL	OPEN INTERVAL	HALF CLOSED/ OPEN INTERVAL
Set Notation	$\{x \mid 0 \leq x \leq 5\}$ endpoint	$\{x \mid 0 < x < 5\}$	$\{x \mid 0 \leq x < 5\}$
Interval Notation	$[\quad , \quad]$	(\quad , \quad)	$[\quad , \quad)$
Number Line	 • Endpoints ___cluded	 • Endpoints ___cluded	

EXAMPLE: Express the set in interval notation & graph on a number line.

$$\{x \mid x \geq 3\}$$



- When solution sets have no “end point,” we use infinity symbols $-\infty$ and ∞ .

- In interval notation, *always* express ∞ with $-\infty$ bounds.

PRACTICE: Express the given set in interval notation and graph.

$$\{x \mid 14 \leq x < 26\}$$



PRACTICE: Express the given interval in set builder notation and graph.

$$(-\infty, 0]$$



TOPIC: LINEAR INEQUALITIES

PRACTICE: Express the given set in interval notation and graph.

$$\{x \mid x \leq 7\}$$



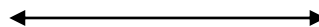
Solving Linear Inequalities

- Linear **inequalities** are just linear **equations** with an _____ symbol instead of an = sign!
 - You can apply **everything** from solving linear equations to linear inequalities.

<u>Linear Equation</u>	<u>Linear Inequality</u>
$\begin{array}{l} 2x - 6 = 0 \\ \quad \cancel{-6} + 6 \\ \hline 2x = 6 \\ \quad \quad \quad \cancel{2} \quad \quad \cancel{2} \\ \hline x = 3 \end{array}$	$\begin{array}{l} 2x - 6 \leq 0 \\ \quad \quad \quad \cancel{-6} + 6 \\ \quad \quad \quad \swarrow \quad \searrow \\ -2x \leq 6 \quad -2x \leq 6 \end{array}$
Solution: _____ value	Multiplying/Dividing by a negative # _____ the symbol. Solution: _____ of values

PRACTICE: Solve the inequality. Express the solution set in interval notation and graph.

$$2x + 12 > 19$$



TOPIC: LINEAR INEQUALITIES

Fractions & Variables on Both Sides

- Solve *inequalities* with **fractions** and/or **variables on both sides** of the symbol just as you would a linear *equation*.

EXAMPLE: Solve the inequality. Express the solution set in interval notation and graph.

$$\frac{1}{4}(x + 2) \geq -\frac{1}{12} - \frac{1}{3}x$$



PRACTICE: Solve the inequality. Express the solution set in interval notation and graph.

$$\frac{1}{3}(x + 1) \geq \frac{1}{5}(3 + 2x)$$

