

## TOPIC: COMPLETING THE SQUARE

- If a quadratic isn't in the form  $(x + \#)^2 = [\text{constant}]$ , you can *put it in that form* by **completing the square**.

$$(x + 3)^2 = 2$$

↓ Square Root Property

$$\sqrt{(x + 3)^2} = \sqrt{2}$$

$$x^2 + 6x + \underline{\hspace{1cm}} = -7 + \underline{\hspace{1cm}}$$

↓ Complete the Square

$$(x + \#)^2 = [\text{constant}]$$

↓ Square Root Property

$$\sqrt{(x + \#)^2} = \sqrt{[\text{constant}]}$$

SOLVING QUADRATIC EQUATIONS			
$ax^2 + bx + c = 0$ (Standard form)			
	FACTORING	SQ. ROOT PROPERTY	COMPLETE THE SQUARE
USE IF	<ul style="list-style-type: none"> <li>Has obvious factors <b>OR</b></li> <li><math>c = 0</math></li> </ul>	<ul style="list-style-type: none"> <li><math>(x + \#)^2 = [\text{constant}]</math> <b>OR</b></li> <li><math>b = 0</math></li> </ul>	<ul style="list-style-type: none"> <li>Leading coeff. (<math>a</math>) is <u>    </u> <b>AND</b></li> <li><math>b</math> is <u>          </u></li> </ul>
STEPS	1) Write eqn in standard form 2) Factor completely 3) Set factors = 0, solve for $x$ 4) Check solutions	1) Isolate squared expression 2) Take + & - square root 3) Solve for $x$ 4) Check solutions	1) Simplify eqn to $x^2 + bx = c$ 2) Add <u>    </u> to <u>both</u> sides 3) Factor to $(x + \underline{\hspace{1cm}})^2$ 4) Solve using <u>                    </u> prop.

**EXAMPLE:** Solve the quadratic equation by completing the square.

(A)

$$x^2 + 6x = -7$$

$$(x + \underline{\hspace{1cm}})^2 =$$

(B)

$$x^2 + 8x + 1 = 0$$

$$(x + \underline{\hspace{1cm}})^2 =$$

$$a^2 + 2ab + b^2 = (a + b)^2$$

(Perfect Square Trinomial)

$$x^2 + bx + \underline{\hspace{1cm}} = c + \underline{\hspace{1cm}}$$

$$(x + \underline{\hspace{1cm}})^2 = [\text{constant}]$$

## TOPIC: COMPLETING THE SQUARE

PRACTICE: Solve the given quadratic equation by completing the square.

$$x^2 + 3x - 5 = 0$$

### COMPLETE THE SQUARE

- 1) Simplify eqn to  $x^2 + bx = c$
- 2)  $+\left(\frac{b}{2}\right)^2$  to both sides
- 3) Factor to  $\left(x + \frac{b}{2}\right)^2$
- 4) Solve using sqrt. prop.

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PRACTICE: Solve the given quadratic equation by completing the square.

$$3x^2 - 6x - 9 = 0$$