

## CONCEPT: INTEGRATED RATE LAW

- **Integrated Rate Law** describes the relationship between [reactants] and \_\_\_\_\_.
  - Helps determine how long it takes for X amount of moles per L of reactant to be \_\_\_\_\_
  - Integrated rate law depends on the \_\_\_\_\_ of the reaction

### Zero-Order Integrated Rate Law

- For reactions following zero order rate law, we use the following equation:

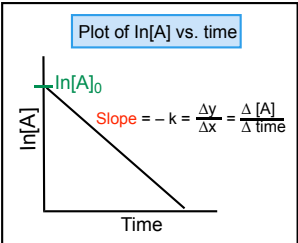
Zero-Order Integrated Rate Law		
<ul style="list-style-type: none"><li>□ <math>[A]_t</math> = Final Reactant Concentration</li><li>□ <math>[A]_0</math> = Initial Reactant Concentration</li><li>□ <math>k</math> = Rate Constant in _____</li><li>□ <math>t</math> = time</li></ul>	$[A]_t = -kt + [A]_0$ <p>Related to equation of a straight line:</p> $y = mx + b$ <p style="text-align: center;">↓</p> <p style="text-align: center;">Slope = <math>-k</math></p>	<p>Plot of <math>[A]</math> vs. time</p> <p>Slope = <math>-k = \frac{\Delta y}{\Delta x} = \frac{\Delta [A]}{\Delta \text{time}}</math></p>

**EXAMPLE:** A plot of  $[\text{NO}_3]$  vs time with a slope of 0.260 gives a straight line. What was the initial concentration of  $\text{NO}_3$  if after 35 seconds its concentration dropped to  $2.75 \times 10^{-2} \text{ M}$ ?

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### First-Order Integrated Rate Law

- For reactions with first order, we use the following equation:

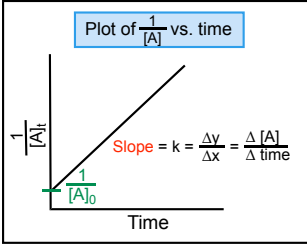
First-Order Integrated Rate Law		
<ul style="list-style-type: none"><li><math>[A]_t</math> = Final Reactant Concentration</li><li><math>[A]_0</math> = Initial Reactant Concentration</li><li><math>k</math> = Rate Constant in _____</li><li><math>t</math> = time</li></ul>	$\ln[A]_t = -kt + \ln[A]_0$ <p>Related to equation of a straight line:</p> $y = mx + b$ <p style="text-align: center;">↓</p> <p style="text-align: center;">Slope = <math>-k</math></p>	<p>Plot of <math>\ln[A]</math> vs. time</p> 

- All \_\_\_\_\_ processes (reactions) follow 1<sup>st</sup> order rate law.

**EXAMPLE:** A certain reaction has a rate constant of  $0.289 \text{ s}^{-1}$ . How long (seconds) would it take for the concentration of reactant A to decrease from  $1.43 \text{ M}$  to  $0.850 \text{ M}$ ?

### Second-Order Integrated Rate Law

- For reactions with second order, we use the following equation:

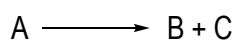
Second-Order Integrated Rate Law		
<ul style="list-style-type: none"><li><math>[A]_t</math> = Final Reactant Concentration</li><li><math>[A]_0</math> = Initial Reactant Concentration</li><li><math>k</math> = Rate Constant in _____</li><li><math>t</math> = time</li></ul>	$\frac{1}{[A]_t} = kt + \frac{1}{[A]_0}$ <p>Related to equation of a straight line:</p> $y = mx + b$ <p style="text-align: center;">↓</p> <p style="text-align: center;">Slope = <math>k</math></p>	<p>Plot of <math>\frac{1}{[A]}</math> vs. time</p> 

**EXAMPLE:** The reactant concentration for a second-order reaction was  $0.670 \text{ M}$  after  $300 \text{ s}$  and  $7.3 \times 10^{-2} \text{ M}$  after  $750 \text{ s}$ . What is the rate constant  $k$  for this reaction?

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**PRACTICE:** For the reaction  $A \longrightarrow B$ , the rate constant is  $0.0837 \text{ M}^{-1}\cdot\text{sec}^{-1}$ . How long would it take for  $[A]$  to decrease by 85%?

**PRACTICE:** The following reaction has a rate constant of  $3.7 \times 10^{-3} \text{ M}\cdot\text{s}^{-1}$  at  $25^\circ\text{C}$ :



Calculate the concentration of C after  $2.7 \times 10^{-3} \text{ sec}$  where  $[A]_0$  was  $0.750 \text{ M}$  at  $25^\circ\text{C}$ ; assume  $[C]_0 = 0 \text{ M}$ .

**PRACTICE:** For the decomposition of urea,  $\text{NH}_2\text{CONH}_2 (\text{aq}) + \text{H}^+(\text{aq}) + 2\text{H}_2\text{O} (\text{l}) \longrightarrow 2\text{NH}_4^+ (\text{aq}) + \text{HCO}_3^- (\text{aq})$ , the rate constant is  $3.24 \times 10^{-4} \text{ s}^{-1}$  at  $35^\circ\text{C}$ . The initial concentration of urea is  $2.89 \text{ mol/L}$ . What fraction of urea has decomposed after 3.5 minutes?

**PRACTICE:** Iodine-123 is used to study thyroid gland function. As this radioactive isotope breaks down, after 5.7 hrs the concentration of iodine-123 is 56.3% complete. Find the rate constant of this reaction.