

CONCEPT: DERIVING THE MULTIPLIER ALGEBRAICALLY

- We can use a simplified aggregate expenditures model to show how the multiplier is derived:
 - The multiplier signifies the multiple increase in GDP based on an initial increase in spending
 - Recall the calculation of the multiplier:

$$Multiplier = \frac{1}{1 - MPC}$$

- To derive it algebraically we start with a **private closed economy** (no government and no international trade)

$$AE = C + I$$
$$AE = A + \overbrace{MPC(YD)}^{C} + I$$

Since there are no taxes or government transfers in this model, then GDP (i.e. national income) = Disposable Income

In equilibrium, $GDP = AE$

Rearrange the formula algebraically and solve for GDP

Analysis: A \$1 increase in spending (from a change in A or I) will result a $1/(1-MPC)$ increase in equilibrium GDP