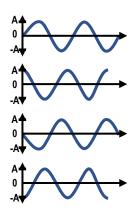
## CONCEPT: WRITING WAVE FUNCTIONS USING THE PHASE CONSTANT

- Sometimes you'll have to write a wave function for a wave that doesn't begin at y=0 or y=±A.
  - We can write ANY wave function by using either

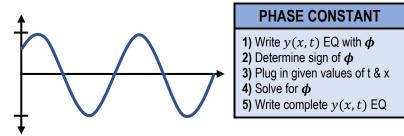
$$y(x,t) = A \sin(kx \pm \omega t \underline{\hspace{1cm}})$$
$$y(x,t) = A \cos(kx \pm \omega t \underline{\hspace{1cm}})$$

 $\phi$  ("phi") = phase constant that "shifts" the graph left/right from its normal starting point.

If graph is shifted RIGHT (+x),  $\phi$  is [+|-] If graph is shifted LEFT (-x),  $\phi$  is [+|-]



<u>EXAMPLE</u>: A transverse wave moving to the right has a wavenumber of 10 rad/m, angular frequency of 62.8 rad/s, and amplitude of 4m. At t = 0, the particle at x = 0 has a displacement of +3m. **a)** Write the wave function using a sine function. **b)** Write the wave function using a cosine function.



• You can write the SAME wave function using sine or cosine, but the phase constant will be DIFFERENT.

<u>PROBLEM</u>: A wave traveling to the right has an Amplitude of 15cm, wavelength of 40cm, and oscillates 8 times per second. At t = 0, the displacement of a particle at x = 0 along this wave is +15cm. Write the wave function, including the phase constant, using a sine function.

**A)** 
$$y(x, t) = 0.15 \sin(0.40x - 8t - 1.57)$$

**B)** 
$$y(x, t) = 0.15 \sin(15.7x + 50.3t)$$

**C)** 
$$y(x, t) = 0.15 \sin(15.7x - 50.3t + 1.57)$$

**D)** 
$$y(x, t) = 0.15 \sin(0.157x - 0.78t - 1.57)$$

## **PHASE CONSTANT**

- 1) Write y(x,t) EQ with  $\phi$
- **2)** Determine sign of  $\phi$
- 3) Plug in given values of t & x
- 4) Solve for  $\phi$
- 5) Write complete y(x, t) EQ