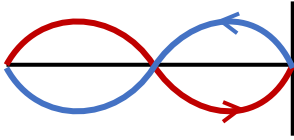


## CONCEPT: STANDING SOUND WAVES

- Longitudinal & Transverse Standing Waves are very similar. Best example: Sound waves in an **open** or **closed** pipe.

### TRANSVERSE STANDING WAVE



- Both ends are [ **Nodes** | **Antinodes** ]

$$f_n = \frac{nv}{2L}$$

$$\lambda_n = \frac{2L}{n}$$

For  $n = 1, 2, 3, \dots$

### LONGITUDINAL STANDING (SOUND) WAVE

#### OPEN PIPE



- Both ends are [ **Open** | **Closed** ]
- Both ends are [ **Nodes** | **Antinodes** ]

$$f_n = \text{---}$$

$$\lambda_n = \text{---}$$

$n = 1, 2, 3, \dots$

#### CLOSED / "STOPPED" PIPE



- 1 end is open, other end [ **Open** | **Closed** ]
- Open end is Antinode, closed end [ **Node** | **Antinode** ]

$$f_n = \text{---}$$

$$\lambda_n = \text{---}$$

$n = 1, 3, 5, \dots$

- For sound waves, *a/ways* assume the speed of sound  $v = 343 \text{ m/s}$  unless otherwise stated.

EXAMPLE: For a particular musical instrument, the pipe which sound travels through is 5m long. **a)** Calculate the fundamental frequency if the pipe is open at both ends. **b)** Calculate the 4<sup>th</sup> overtone if the pipe is open at 1end, closed at the other.

**PROBLEM:** The fundamental frequency of your *closed* organ pipe is 200 Hz. The second overtone of this pipe has the same frequency as the 3<sup>rd</sup> harmonic of an *open* pipe. What is the length of this open pipe?

- A) 0.85 m
- B) 0.51 m
- C) 0.69 m
- D) 0.43 m

### STANDING WAVES

$$v = \sqrt{\frac{F_T}{\mu}} \text{ (for strings only)}$$

$$f_1 = \frac{v}{2L}$$

$$f_n = nf_1 = \frac{nv}{2L} \text{ (open pipe)}$$

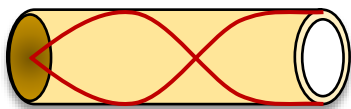
$$\lambda_n = \frac{2L}{n} \text{ (open pipe)}$$

$$f_n = nf_1 = \frac{nv}{4L} \text{ (closed pipe)}$$

$$\lambda_n = \frac{4L}{n} \text{ (closed pipe)}$$

$$n^{\text{th}} \text{ Overtone} = (n+1)^{\text{th}} \text{ Harmonic}$$

**PROBLEM:** The length of the closed pipe shown below is 2.75 m long. **a)** Calculate the frequency of the standing wave shown. **b)** Calculate the fundamental frequency of the pipe.



### STANDING WAVES

$$v = \sqrt{\frac{F_T}{\mu}} \text{ (for strings only)}$$

$$f_1 = \frac{v}{2L}$$

$$f_n = nf_1 = \frac{nv}{2L} \text{ (open pipe)}$$

$$\lambda_n = \frac{2L}{n} \text{ (open pipe)}$$

$$f_n = nf_1 = \frac{nv}{4L} \text{ (closed pipe)}$$

$$\lambda_n = \frac{4L}{n} \text{ (closed pipe)}$$

$$n^{\text{th}} \text{ Overtone} = (n+1)^{\text{th}} \text{ Harmonic}$$