

CONSERVATION OF ENERGY / ROLLING MOTION

- Remember: If an object moves while rotating (Rolling Motion) on a surface without slipping $\rightarrow v_{CM} = \underline{\hspace{2cm}}$
 - In order for an object to start rotating, or to rotate faster (α), there needs to be $\underline{\hspace{2cm}}$ (τ).
 - The role of $\underline{\hspace{2cm}}$ in Rolling Motion is to “convert” some $\underline{\hspace{1cm}}$ into $\underline{\hspace{1cm}}$ ($\underline{\hspace{1cm}}$ into $\underline{\hspace{1cm}}$).
 - Unless otherwise stated, $\underline{\hspace{2cm}}$ does this without dissipating any energy $\rightarrow W_{\text{fric}} = \underline{\hspace{2cm}}$
 - To summarize: If $\alpha \neq 0 \rightarrow$ there is $\underline{\hspace{2cm}}$ but $\underline{\hspace{2cm}}$.
If “without slipping” \rightarrow there is $\underline{\hspace{2cm}}$.

EXAMPLE: A solid cylinder of mass M and radius R is released from rest from the top of an inclined plane of length L that makes an angle of Θ with the horizontal. The cylinder rolls without slipping. Derive expressions for the linear and angular speeds that the cylinder will have at the bottom of the plane.

PRACTICE: SPHERE GOING UP A HILL / MAX HEIGHT

PRACTICE: A solid sphere of mass $M = 10 \text{ kg}$ and radius $R = 2$ is rolling without slipping with speed $V = 5 \text{ m/s}$ on a flat surface when it reaches the bottom of an inclined plane that makes an angle of $\Theta = 37^\circ$ with the horizontal. The plane has just enough friction to cause the sphere to roll without slipping while going up. What maximum height will the sphere attain?

EXAMPLE: ROLLING SPHERE / ROUGH AND SMOOTH HILLS

EXAMPLE: A solid sphere of mass M and radius R is initially at rest at the top of a rough hill of height H_1 . The sphere rolls down the rough hill, then rides on a smooth horizontal surface, then goes up a long, smooth hill. The first hill (rough) has enough friction to cause the sphere to roll without slipping. What maximum height H_2 , in terms of H_1 and other variables, will the sphere attain on the second hill (smooth)?

→ BONUS: Why are the two heights different?

PRACTICE: SPHERE ON LOOP-THE-LOOP / SPEED AT BOTTOM

PRACTICE: You may remember that the lowest speed that an object may have at the top of a loop-the-loop of radius R , so that it completes the loop without falling, is \sqrt{gR} . Calculate the lowest speed that a solid sphere must have at the bottom of a loop-the-loop, so that it reaches the top with enough speed to complete the loop. Assume the sphere rolls without slipping.