

## CONCEPT: LINEAR THERMAL EXPANSION

- **Thermal Expansion:** If you increase the temperature of most materials, their \_\_\_\_\_ also increases (i.e. they expand).
  - For roughly 1D objects (like a rod), changing temperature ( $\Delta T$ ) also changes the \_\_\_\_\_ ( $\Delta L$ ) of the rod.

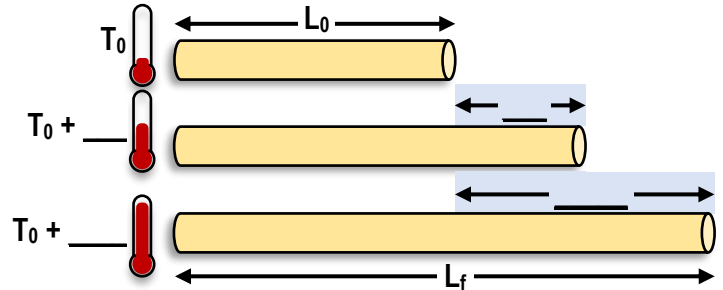
$$\Delta L = \underline{\hspace{2cm}}$$

$\alpha$  = coefficient of linear expansion [ Units:  $\frac{1}{K}$  or  $\frac{1}{^{\circ}C}$  ]

$L_0$  = initial length of object

- Sometimes you'll have to calculate the final length  $L_f$ .
  - We can use  $\Delta L = L_f - L_0$  to write an EQ for  $L_f$ :

$$L_f = \underline{\hspace{2cm}}$$



**EXAMPLE:** An aluminum metal rod has an initial length of exactly 50.000m at an initial temperature of 20°C. If the coefficient of linear expansion for aluminum is  $2.4 \times 10^{-5}$ , **a)** by how much does the length of the rod increase if you heat it up to 35°C? **b)** What would the final length of the rod be if you continued heating it up to 50°C?

- $\Delta T$  is the **same** in K and  $^{\circ}C$ , so we can use either  $\Delta T_K$  or  $\Delta T_C$  in these equations.

**PROBLEM:** On a very cold day at a temperature of  $-12^{\circ}\text{C}$ , a power line made of aluminum between two support towers measures exactly 150.56m. You go out on a hot day and measure the power line to be exactly 150.71m. What is the temperature (in  $^{\circ}\text{C}$ ) outside? The linear expansion coefficient of aluminum is  $2.4 \times 10^{-5}$ .

- A)  $29.5^{\circ}\text{C}$
- B)  $-11.8^{\circ}\text{C}$
- C)  $41.7^{\circ}\text{C}$

<b>LINEAR THERMAL EXPANSION</b>
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$\Delta L = \alpha L_0 \Delta T$
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$L_f = L_0(1 + \alpha \Delta T)$
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**PROBLEM:** Steel measuring tape is usually calibrated for measurement accuracy at  $20^{\circ}\text{C}$ . If the measuring tape is exactly 50m long at this temperature, what is the length of the tape at  $40^{\circ}\text{C}$ ? The linear expansion coefficient of steel is  $1.2 \times 10^{-5}$ .

<b>LINEAR THERMAL EXPANSION</b>
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$\Delta L = \alpha L_0 \Delta T$
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$L_f = L_0(1 + \alpha \Delta T)$
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