CONCEPT: CONSERVATION OF MECHANICAL ENERGY

• Mechanical Energy (**ME**) of a system is simply the _____ of Kinetic (**K**) & Potential (**U**) energy:

ME = K + U

<u>EXAMPLE</u>: You drop a 2kg ball from the top of a 100m building. Calculate the ball's total Mechanical Energy **a)** at the top of the building and then **b)** at the moment right before it hits the ground.



Energy
$$K = \frac{1}{2}mv^2$$

$$U_g = mgy$$

UAM Equations

$$(1) v = v_0 + at$$

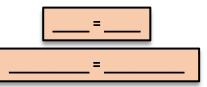
$$(2) v^2 = v_0^2 + 2a\Delta x$$

$$(3) \Delta x = v_0 t + \frac{1}{2} a t^2$$

$$(4) \Delta x = \left(\frac{\nu + \nu_0}{2}\right) x$$

• When a system's **M.E.** is transferred between potential & kinetic energy <u>without loss</u>, we say it is _____:

...which we will always write as:



(Conservation of Mechanical Energy)

<u>EXAMPLE</u>: You drop a ball of unknown mass from the top of a 50m building. Use <u>Conservation of Energy</u> to determine the speed of the ball right before it hits the ground.

CONSERVATION OF ENERGY

- 1) Draw Diagram
- 2) Write Cons. of Energy EQ
- 3) Eliminate & expand terms
- 4) Solve

<u>PROBLEM</u>: You launch a 4kg object directly up from the ground with an initial 40m/s. Use Energy Conservation to find the maximum height the object reaches. Ignore air resistance.

CONSERVATION OF ENERGY

- 1) Draw Diagram
- 2) Write Cons. of Energy EQ
- 3) Eliminate & expand terms
- 4) Solve

<u>PROBLEM</u>: You throw a 6kg object down from a height of 20m. If the object reaches the ground with 30m/s, calculate the initial speed you threw it with.

CONSERVATION OF ENERGY

- 1) Draw Diagram
- 2) Write Cons. of Energy EQ
- 3) Eliminate & expand terms
- 4) Solve

UAM Equations

$$(1) v = v_0 + at$$

(2)
$$v^2 = v_0^2 + 2a\Delta x$$

$$(3) \Delta x = v_0 t + \frac{1}{2} a t^2$$

$$(4) \Delta x = \left(\frac{v + v_0}{2}\right) \mathbf{t}$$

PROBLEM: You launch a ball directly upward from the ground.	The ball is going up with	20m/s at 30m from the ground. a)
Calculate the launch speed. b) Calculate its maximum height.		
		CONSERVATION OF ENERGY

- 1) Draw Diagram
 2) Write Cons. of Energy EQ
 3) Eliminate & expand terms
- 4) Solve

• Some problems give more than TWO points. The 2 points you pick should be the **GIVEN** & **TARGET** (known & unknown)

CONCEPT: CONSERVATION OF TOTAL ENERGY AND ISOLATED SYSTEMS

• There are 2 conceptual rules explaining when Energy is conserved:

TOTAL ENERGY			
Mechanical Energy		Non-Mech. Energy	
Kinetic	Potential		Thermal (friction)
	Elastic	Grav.	+ all other types

Total Energy

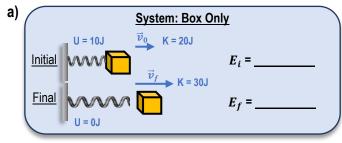
1) The TOTAL Energy of a system is conserved if the system is ____

- A *system* is a _____ of objects that is CHOSEN (by you or the problem).
- A system is **ISOLATED** if NO External forces do work and ONLY Internal forces do work.
- External Forces are [inside | outside] of system. If ANY Net Force is external, system is [isolated | not isolated]

All Forces

- <u>Internal</u> Forces are [inside | outside] of system. If ALL Forces are internal, system is [isolated | not isolated]

<u>EXAMPLE</u>: A spring pushes a box, and it accelerates. Determine whether the (i) forces are internal, (ii) system is isolated, and (iii) Total Energy of the system is conserved if the system is defined as a) only the box; b) the box AND the spring.



b)	System: Box + Spring			
		U = 10J	\overrightarrow{v}_0 K = 20J	_
	<u>Initial</u>		\overrightarrow{v}_f K = 30J	$E_i = \underline{\hspace{1cm}}$
	<u>Final</u>	VVV		$E_f = \underline{\hspace{1cm}}$
	(U = 0J	_	

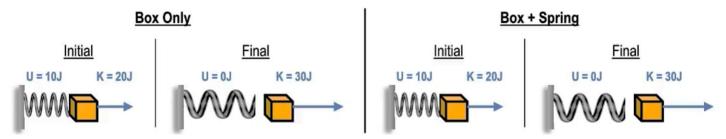
internal?	Isolated?	Conserved?	
		$E_i \underline{\hspace{1cm}} E_f$	
		E_i E_f	

System

CONCEPT: SYSTEMS AND CONSERVATIVE VS. NON-CONSERVATIVE FORCES

• Conservation of Energy often refers to a ______ of objects that is CHOSEN.

<u>EXAMPLE</u>: Consider spring pushing a box. Determine whether the Mechanical Energy of the system is conserved if the system is defined as **a**) only the box; **b**) the box AND the spring.



• Mech. Energy in a system is **CONSERVED** if the ONLY forces doing work are ______ Forces. (_____ = 0)

EXAMPLE: For each of the situations below: (i) Is the mechanical energy conserved? (ii) Describe the energy transfers.

SITUATION	Energy Conserved?	Energy Transfers
(a) A block falls without air resistance		
(b) A moving block hits a spring, deforms it, and rebounds		
(c) You push a block at rest, and it accelerates to the right		
(d) A moving block slows due to friction		

CONSERVATIVE FORCES		NON-CONSERVATIVE FORCES ● Mechanical Energy is	
Gravity (a.k.a Weight)	Spring (Hooke's Law)	Applied Forces	Friction
v ↑ v ↑			

• Conservative Forces are "_____", meaning you can "undo" the action and get any lost energy back.