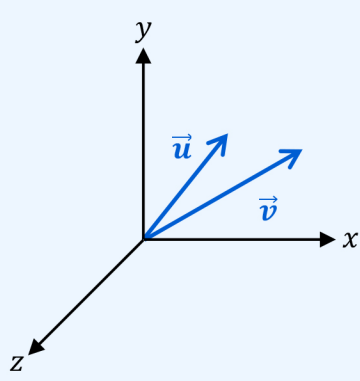
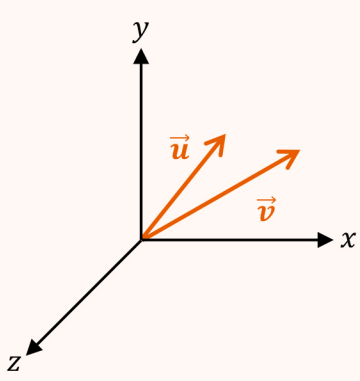


TOPIC: CROSS PRODUCT

Computing the Cross Product

◆ Like the dot product, the **cross product** is a way to _____ vectors.

Recall	Dot Product	New	Cross Product
	 <p>$\vec{u} \cdot \vec{v} = [\text{SCALAR} \mid \text{VECTOR}]$</p>		 <p>ALWAYS _____ to original vectors</p> <p>$\vec{u} \times \vec{v} = [\text{SCALAR} \mid \text{VECTOR}]$</p>

EXAMPLE

Find the cross product, $\vec{w} = \vec{u} \times \vec{v}$.

$$\vec{u} = \langle 2, 0, 1 \rangle \quad \vec{v} = \langle 0, -1, 2 \rangle$$

$$\vec{u} \times \vec{v} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 0 & 1 \\ 0 & -1 & 2 \end{vmatrix} = \begin{vmatrix} _ & _ & _ \\ _ & _ & _ \\ _ & _ & _ \end{vmatrix}$$

$$w_x = u_y v_z - v_y u_z = _ = _$$

$$w_y = _ = _ = _$$

$$w_z = _ = _ = _$$

$$\vec{w} = (_) \hat{i} + (_) \hat{j} + (_) \hat{k}$$

HOW TO: Calculate Cross Product

1) Write matrix of each vector's $\hat{i}, \hat{j}, \hat{k}$ components

2) Repeat \hat{i}, \hat{j} columns outside matrix

For each \vec{w} component:

3) Write $u v - v u$

4) Multiply “_____” components diagonally ()

TOPIC: CROSS PRODUCT

PRACTICE

If vectors $\vec{v} = \langle 3, 1, 0 \rangle$, $\vec{u} = \langle 0, -2, 0 \rangle$ and $\vec{w} = \vec{v} \times \vec{u}$, find \vec{w} .

$$\begin{array}{l} \vec{v} \\ \vec{u} \end{array} \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \text{---} & \text{---} & \text{---} \\ \text{---} & \text{---} & \text{---} \end{vmatrix} \begin{vmatrix} \hat{i} & \hat{j} \\ \text{---} & \text{---} \\ \text{---} & \text{---} \end{vmatrix}$$

PRACTICE

If vectors $\vec{a} = 5\hat{i}$, $\vec{b} = 12\hat{k}$ and $\vec{c} = \vec{a} \times \vec{b}$, find \vec{c} .