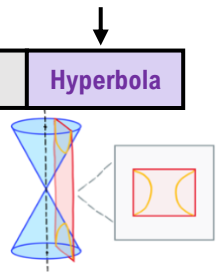


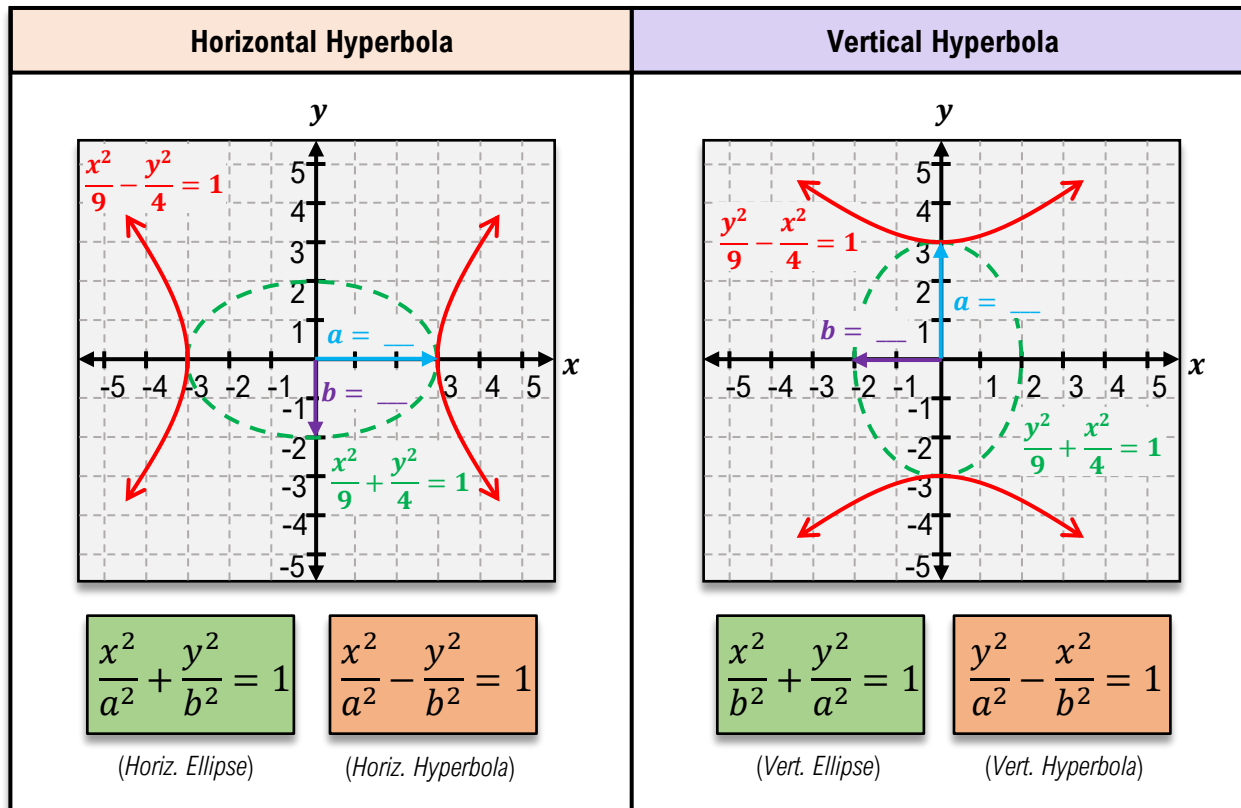
TOPIC: Hyperbolas at the Origin

Introduction to Hyperbolas

Circle	Ellipse	Parabola	Hyperbola
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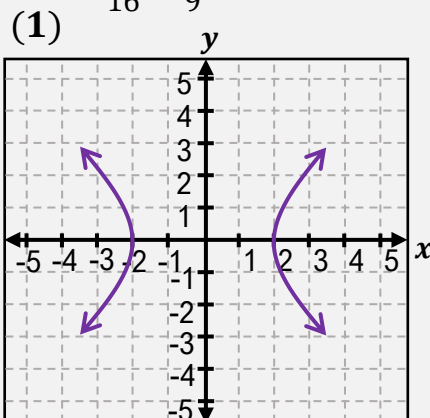
- The equation for a hyperbola is the same as an ellipse, but with a ____.
- Visually, a hyperbola appears as two _____ facing away from each other.



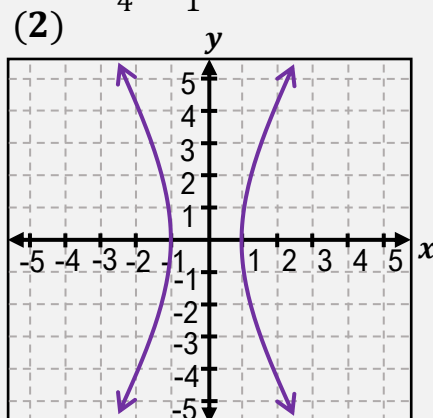
- The axis major axis (a) is always [**LARGEST | FIRST**] for an ellipse, and [**LARGEST | FIRST**] for a hyperbola.

EXAMPLE: Match the equation to the graph

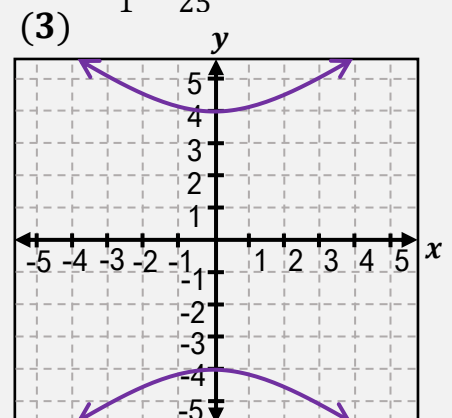
(A) $\frac{y^2}{16} - \frac{x^2}{9} = 1$



(B) $\frac{x^2}{4} - \frac{y^2}{1} = 1$



(C) $\frac{x^2}{1} - \frac{y^2}{25} = 1$



TOPIC: Hyperbolas at the Origin

PRACTICE: Given the hyperbola $\frac{x^2}{25} - \frac{y^2}{9} = 1$, find the length of the a-axis and b-axis.

(A) $a = 25, b = 9$

(B) $a = 9, b = 25$

(C) $a = 5, b = 3$

(D) $a = 3, b = 5$

PRACTICE: Given the hyperbola $x^2 - \frac{y^2}{4} = 1$, find the length of the a-axis and b-axis.

(A) $a = 1, b = 4$

(B) $a = 4, b = 1$

(C) $a = 1, b = 2$

(D) $a = 2, b = 1$

TOPIC: Hyperbolas at the Origin

PRACTICE: Given the hyperbola $\frac{y^2}{100} - \frac{x^2}{139} = 1$, find the length of the a-axis and b-axis.

(A) $a = 100, b = 139$

(B) $a = 139, b = 100$

(C) $a = \sqrt{139}, b = 10$

(D) $a = 10, b = \sqrt{139}$

TOPIC: Hyperbolas at the Origin

Vertices and Foci of Hyperbolas

Circle	Ellipse	Parabola	Hyperbola
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- Every hyperbola has 2 **Vertices** & 2 **Foci**, both located on the [**MAJOR** | **MINOR**] axis.

- **Vertices** are the points on the hyperbola _____ to the center

Distance between center & **Vertex** = [**a** | **b** | **c**]

- For any point on a hyperbola, the _____ of the distances between the point & each **Focus** is a constant

Distance between center & **Focus** = [**a** | **b** | **c**]

$$c^2 = a^2 - b^2$$

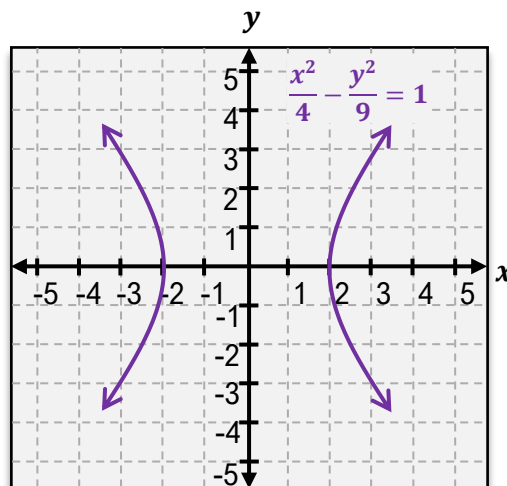
(Foci of Ellipse)

$$c^2 = a^2 + b^2$$

(Foci of Hyperbola)

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

(Horiz. Hyperbola)



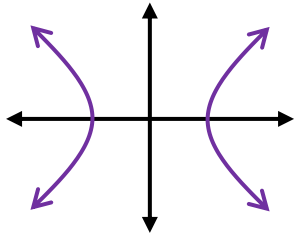
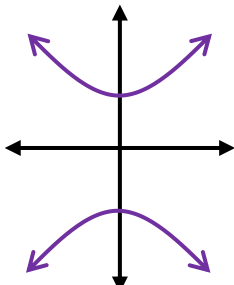
EXAMPLE: Find the vertices & foci of the hyperbola in the graph.

a =

b =

c =

- For a *vertical* hyperbola, the coordinates of vertices & foci are different

Horizontal Hyperbola	Vertical Hyperbola
 Vertices: (__ , 0) & (__ , 0) Foci: (__ , 0) & (__ , 0) Vertices & Foci on [x y] axis	 Vertices: (0 , __) & (0 , __) Foci: (0 , __) & (0 , __) Vertices & Foci on [x y] axis

TOPIC: Hyperbolas at the Origin

PRACTICE: Determine the vertices and foci of the hyperbola $\frac{y^2}{4} - x^2 = 1$.

- (A) Vertices: $(2,0), (-2,0)$
Foci: $(\sqrt{5}, 0), (-\sqrt{5}, 0)$
- (B) Vertices: $(0,2), (0,-2)$
Foci: $(0, \sqrt{5}), (0, -\sqrt{5})$
- (C) Vertices: $(1,0), (-1,0)$
Foci: $(5,0), (-5,0)$
- (D) Vertices: $(0,1), (0,-1)$
Foci: $(0,5), (0,-5)$

PRACTICE: Find the equation for a hyperbola with a center at $(0,0)$, focus at $(0,-6)$ and vertex at $(0,4)$.

- (A) $\frac{y^2}{16} - \frac{x^2}{20} = 1$
- (B) $\frac{y^2}{20} - \frac{x^2}{16} = 1$
- (C) $\frac{y^2}{4} - \frac{x^2}{\sqrt{20}} = 1$
- (D) $\frac{y^2}{\sqrt{20}} - \frac{x^2}{4} = 1$

TOPIC: Hyperbolas at the Origin

Asymptotes of Hyperbolas

- To graph hyperbolas, you'll need asymptotes

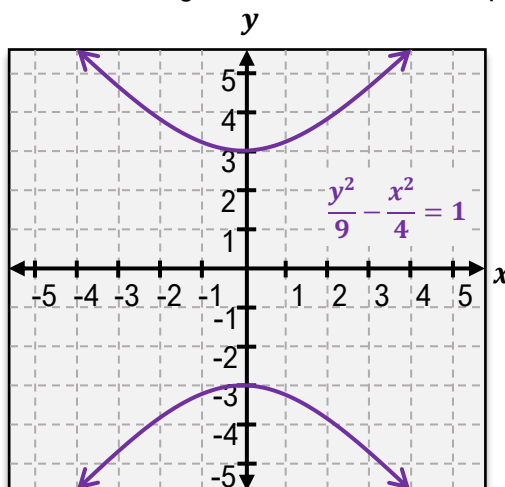
- The values of a & b form a _____ where the asymptotes are drawn through the corners of the shape.

$$\frac{y^2}{a^2} - \frac{x^2}{b^2} = 1$$

(Vert. Hyperbola)

$$y = \pm \frac{a}{b}x$$

(Vert. Hyperbola Asym.)



EXAMPLE: Find & draw the asymptotes of the given hyperbola.

$a =$

$b =$

Asymptotes: $y =$ _____ & $y =$ _____

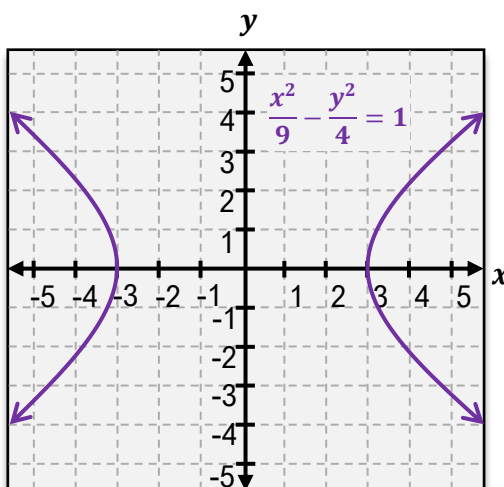
- For asymptotes of horizontal hyperbolas, just flip a & b

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

(Horiz. Hyperbola)

$$y = \pm \frac{a}{b}x$$

(Horiz. Hyperbola Asym.)



EXAMPLE: Find & draw the asymptotes of the given hyperbola.

$a =$

$b =$

Asymptotes: $y =$ _____ & $y =$ _____

TOPIC: Hyperbolas at the Origin

PRACTICE: Find the equations for the asymptotes of the hyperbola $\frac{x^2}{64} - \frac{y^2}{100} = 1$.

(A) $y = \pm \frac{4}{5}x$

(B) $y = \pm \frac{5}{4}x$

(C) $y = \pm \frac{16}{25}x$

(D) $y = \pm \frac{25}{16}x$

PRACTICE: Find the equations for the asymptotes of the hyperbola $\frac{y^2}{16} - \frac{x^2}{9} = 1$.

(A) $y = \pm \frac{9}{16}x$

(B) $y = \pm \frac{16}{9}x$

(C) $y = \pm \frac{3}{4}x$

(D) $y = \pm \frac{4}{3}x$

TOPIC: Hyperbolas at the Origin

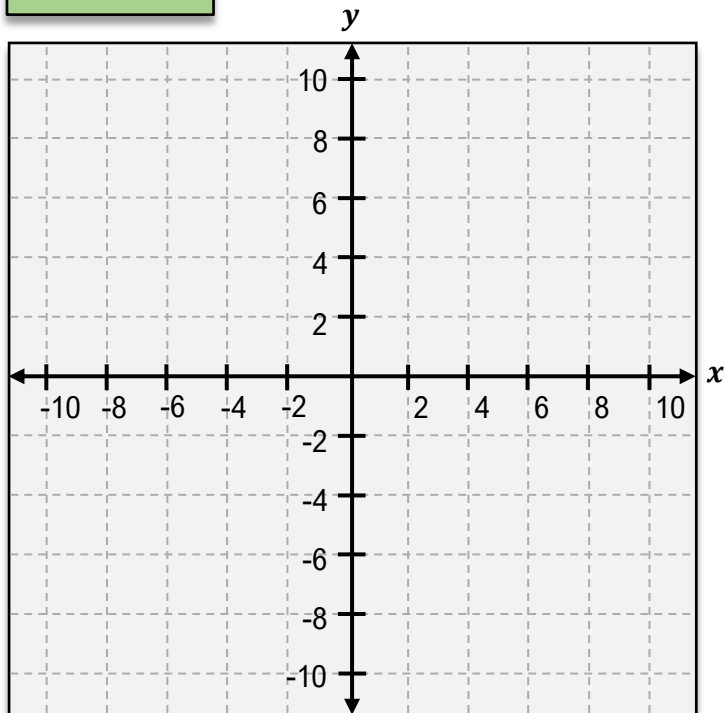
Graph Hyperbolas at the Origin

EXAMPLE: Graph the hyperbola and identify the foci.

↓

Circle	Ellipse	Parabola	Hyperbola
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$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$



	$\frac{x^2}{9} - \frac{y^2}{64} = 1$
TO GRAPH	1) Hyperbola is [HORIZONTAL VERTICAL] 2) Vertices $(\pm a, 0)$, OR $(0, \pm a)$: $(_, _) & (_, _)$ 3) b points $(\pm b, 0)$, OR $(0, \pm b)$: $(_, _) & (_, _)$ 4) Asymptotes: (A) draw a box through vertices & b points (B) draw lines through box corners 5) Draw branches at vertices & approaching asym.
FROM GRAPH	6) Foci $(\pm c, 0)$, OR $(0, \pm c)$: $c^2 = a^2 + b^2$ $(_, _) & (_, _)$

TOPIC: Hyperbolas at the Origin

EXAMPLE: Graph the hyperbola and identify the foci.

$$\frac{x^2}{16} - \frac{y^2}{20} = 1$$

TO GRAPH

1) Hyperbola is [**HORIZONTAL** | **VERTICAL**]

2) **Vertices** $(\pm a, 0)$, OR $(0, \pm a)$:

(__, __) & (__, __)

3) **b points** $(\pm b, 0)$, OR $(0, \pm b)$:

(__, __) & (__, __)

4) Asymptotes:

(A) draw a box through **vertices** & **b points**

(B) draw lines through box corners

5) Draw branches at **vertices** & approaching asym.

FROM GRAPH

6) Foci $(\pm c, 0)$, OR $(0, \pm c)$:

(__, __) & (__, __)

