

## TOPIC: SOLVING LINEAR EQUATIONS

- A **linear expression** with an \_\_\_\_ sign is a **linear equation**!

### Linear Expression

$$2x + 3$$

When  $x$  is 4,

$$\underbrace{2(4) + 3}_{11}$$

- Simplify/evaluate for **KNOWN**  $x$

### Linear Equation

$$2x + 3 \underline{\hspace{1cm}}$$

- Solve for **UNKNOWN**  $x$ 
  - Find value(s) of  $x$  that make the statement \_\_\_\_\_

- You will need to use different operations (+, −, ×, ÷) to \_\_\_\_\_  $x$ .
  - These operations should **ALWAYS** be done to \_\_\_\_\_ of the equation.

EXAMPLE: Identify and perform the operation needed to **isolate**  $x$  by applying it to both sides.

(A)  $x + 2 = 0$

(B)  $3x = 12$

### Operations

\_\_\_\_\_  
+  
×

- You'll often have to do *multiple* operations to solve a linear equation.

EXAMPLE: Solve the equation.

$$2(x - 3) = 0$$

Simplifying  
Algebraic  
Expressions

### SOLVING LINEAR EQUATIONS

- 1) Distribute constants
- 2) Combine like terms
- 3) Group terms w/ \_\_\_\_ & \_\_\_\_\_ on opposite sides
- 4) Isolate  $x$  (Solve for  $x$ )
- 5) \_\_\_\_\_ solution by replacing  $x$  in original equation

- \_\_\_\_ is the \_\_\_\_\_ or \_\_\_\_\_ of the equation

## TOPIC: SOLVING LINEAR EQUATIONS

PRACTICE: Solve the equation.

$$3(2 - 5x) = 4x + 25$$

### **SOLVING LINEAR EQUATIONS**

- 1) Distribute constants
- 2) Combine like terms
- 3) Group terms w/  $x$  & constants on opposite sides
- 4) Isolate  $x$
- 5) Check solution by replacing  $x$  in original equation

## Linear Equations with Fractions

- Linear equations may have **fractions** that need to be \_\_\_\_\_ using **L**east **C**ommon **D**enominator first.

EXAMPLE: Solve the equation.

$$\frac{1}{4}(x + 2) - \frac{1}{3}x = \frac{1}{12}$$

### **SOLVING LINEAR EQUATIONS**

- 0) Multiply by \_\_\_\_\_ to eliminate fractions
- 1) Distribute constants
- 2) Combine like terms
- 3) Group terms w/  $x$  & constants on opposite sides
- 4) Isolate  $x$
- 5) (Optional) Check by replacing  $x$  in original eqn

PRACTICE: Solve the equation.

$$\frac{9}{2} + \frac{1}{4}(x + 2) = \frac{3}{4}x$$

## TOPIC: SOLVING LINEAR EQUATIONS

### Categorizing Linear Equations

• **Linear equations** can be put in 3 possible **categories** based on \_\_\_\_\_ solutions they have.

- These solutions may be written as a \_\_\_\_\_.

EXAMPLE: Solve, then categorize the linear equations.

_____	_____	_____
$2x + 4 = 10$	$x + 5 = x + 2 + 3$	$x = x + 4$
<ul style="list-style-type: none"><li>• _____ <b>solution</b></li><li>• Solution set is _____</li></ul>	<ul style="list-style-type: none"><li>• _____ statement</li><li>• _____ <b>solutions</b></li><li>• Solution set is _____ (all real numbers)</li></ul>	<ul style="list-style-type: none"><li>• _____ statement</li><li>• _____ solutions</li><li>• Solution set is _____, _____ set</li></ul>

PRACTICE: Solve the equation. Then state whether it is an identity, conditional, or inconsistent equation.

$$5x + 17 = 8x + 12 - 3(x + 4)$$

#### **SOLVING LINEAR EQUATIONS**

- 0) Multiply by LCD to eliminate fractions
- 1) Distribute constants
- 2) Combine like terms
- 3) Group terms w/  $x$  & constants on opposite sides
- 4) Isolate  $x$  (if any  $x$  terms remain)

## **TOPIC: SOLVING LINEAR EQUATIONS**

**PRACTICE:** Solve the equation. Then state whether it is an identity, conditional, or inconsistent equation.

$$\frac{x}{4} + \frac{1}{6} = \frac{x}{3}$$

### **SOLVING LINEAR EQUATIONS**

- 0)** Multiply by LCD to eliminate fractions
- 1)** Distribute constants
- 2)** Combine like terms
- 3)** Group terms w/  $x$  & constants on opposite sides
- 4)** Isolate  $x$  (if any  $x$  terms remain)

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**PRACTICE:** Solve the equation. Then state whether it is an identity, conditional, or inconsistent equation.

$$-2(5 - 3x) + x = 7x - 10$$